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Electrostatics

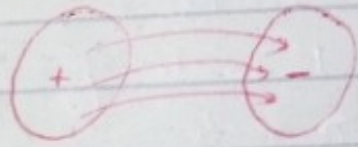
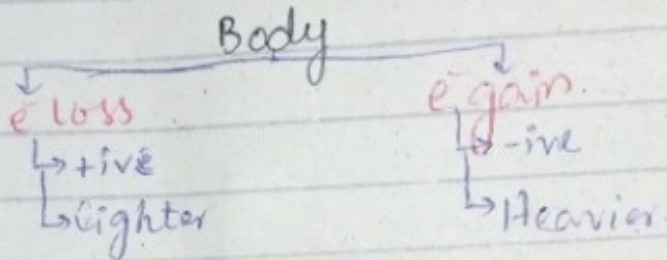
charges at rest

What is charge?

↳ still unknown

"intrinsic property of matter"

Electron⁻ Positron⁺



What is 1C?

→ Quantization of charge.

$$q = ne$$

↳ e = elementary charge

1e = minimum value of charge on e.

$$1e = 1.6 \times 10^{-19} \text{ C}$$

$$1e = 16 \times 10^{-20} \text{ C}$$

$$q = 1 \text{ C}, n = ?$$

$$n = \frac{q}{e} = \frac{1 \text{ C}}{16 \times 10^{-20} \text{ C}}$$

@isamiqamar

$$n = 6.25 \times 10^{18} \text{ es}$$

$$1 \text{ C} = 6.25 \times 10^{18} \text{ es}$$

$$1 \text{ C} = \frac{6.25 \times 10^{18}}{10^6} \text{ es}$$

$$1 \text{ C} = 625 \text{ 0000 0000 0000 0000 es}$$

$$1 \text{ C} = 6 \times 10^{18} \text{ e}$$

$$1 \text{ C} = 6.25 \times 10^{18}$$

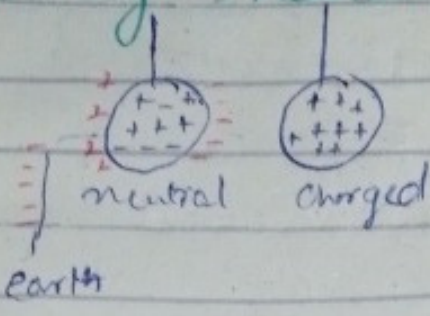
Charging Method:

i. By Friction:

Combing

11

ii: By Induction:

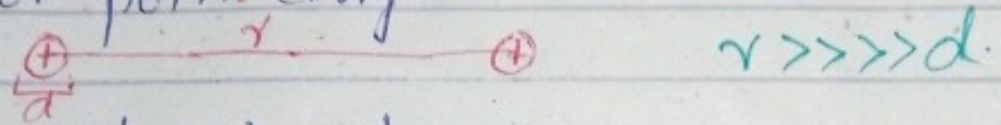


Gold leaf electroscope.

Coulombs Law:

Limitation:

↳ for point charges.



↳ must be at rest

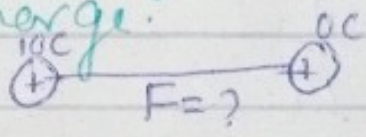
↳ Inside nucleus not applicable.

$$F \propto q_1 q_2$$

$$F \propto \frac{1}{r^2}$$

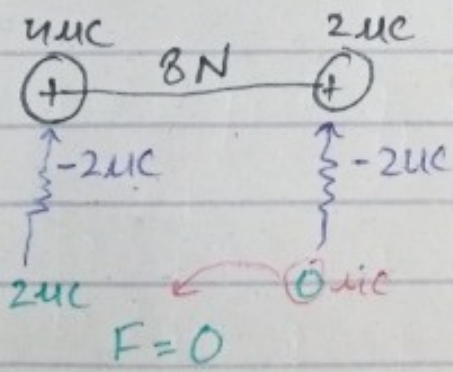
$$F = \frac{k q_1 q_2}{r^2}$$

∴ Force depends upon product of charges not on single charge.



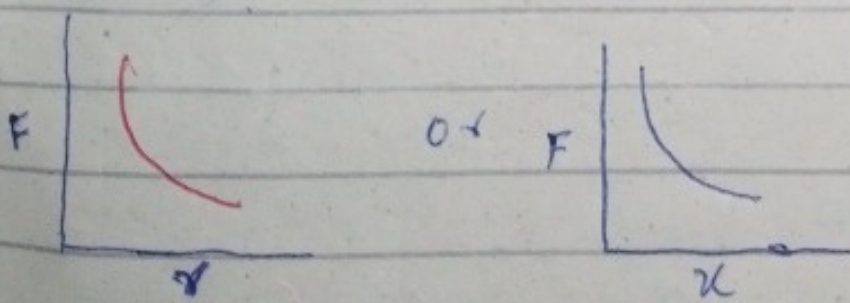
$$F = q_1 q_2 = 0$$

↳ if one charge is zero the force will become zero



@isamiqamar

$$F \propto \frac{1}{r^2}$$



Let $k=1$:

• $q_1 = 2q, q_2 = 2q, r$ same
 $F' = \frac{k(2q)(2q)}{r^2}$

$F' = 4F$

• $q_1 = q_2 = \text{same}, r = 2r$
 $F = \frac{1}{4} F$

• $r = \frac{1}{2} r$

$F' = 4F$

• $q_1 = 2q, q_2 = 2q, r = 2r$
 $F' = \frac{(2q)(2q)}{(2r)^2}$

$F' = \text{same}$

mcq: For what value of r Force becomes half.

a: $2r$

b: $\frac{r}{2}$

c: $\sqrt{2}r$

d: none

$F = \frac{kq_1q_2}{r^2}$

$k = \text{Coulomb's constant}$

$k = \frac{1}{4\pi\epsilon} = \frac{1}{4\pi\epsilon_0\epsilon_r} \quad \therefore \epsilon = \epsilon_0\epsilon_r$

Vacuum

$\epsilon_r = 1$

$k_{vac} = \frac{1}{4\pi\epsilon_0}$

Medium

$\epsilon_r \neq 1$

$k_m = \frac{1}{4\pi\epsilon_0\epsilon_r}$

$\epsilon_0 = \text{Permittivity of free space}$

$= 8.85 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$

$k_{vac} = \frac{1}{4(3.14)(8.85 \times 10^{-12})}$

$k_{vac} = 9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2}$

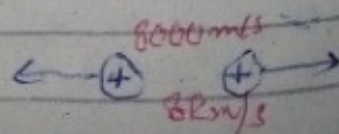
$F = \frac{Gm_1m_2}{r^2}$

$G = 6.67 \times 10^{-11}$

$F = \frac{kq_1q_2}{r^2}$

$k = 9 \times 10^9$

$k > G$



Dependance of K :

1: medium:

$$K_m = \frac{1}{4\pi \epsilon_0 \epsilon_r}$$

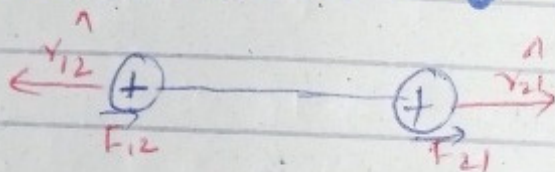
$$\epsilon_r = 2, 4, 80$$

2: System of units:

$$K = 9 \times 10^9 \text{ (SI)}$$

$$K = 1 \text{ (G.G.S)}$$

Vector Form of Coulombs law:



$$\hat{r}_{12} = -\hat{r}_{21}$$

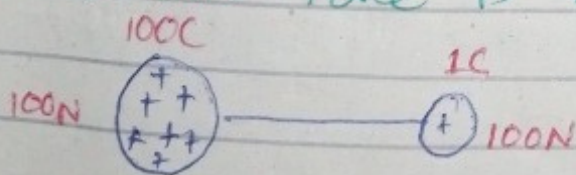
$$\vec{F}_{12} = -\vec{F}_{21}$$

magnitude:

$$F_{12} = F_{21}$$

$$\# \frac{F_{12}}{F_{21}} = \frac{1}{1} \quad | : |$$

* Coulombs force is mutual force.



→ The force will remain same on both charges as it does not depend on individual charge.

$$\frac{F_1}{F_2} = \frac{1}{1}$$

Effect of Medium:

$$F_{vac} = k_{vac} \frac{q_1 q_2}{r^2}$$

$$F_{vac} = \frac{1}{4\pi \epsilon_0} \frac{q_1 q_2}{r^2} \quad \text{--- (1)}$$

$$F_{med} = k_m \frac{q_1 q_2}{r^2}$$

$$F_m = \frac{1}{4\pi\epsilon_0\epsilon_r} \frac{q_1 q_2}{r^2} \quad \text{--- ①}$$

$$F_m = \frac{F_{vac}}{\epsilon_r}$$

$\epsilon_r = ?$ (Relative permittivity)

$$\epsilon_r = \frac{F_v}{F_m}$$

nncq:

$$F_{vac} = 100 \text{ N}$$

$$\epsilon_r = 2$$

$$F_{med} = ?$$

$$F_{med} = \frac{100}{2}$$

$$F_m = 50 \text{ N}$$

nncq:

$$F_m = 100$$

$$F_v = 5$$

$$\epsilon_r = ?$$

$$\epsilon_r = \frac{5}{10} = \frac{1}{2}$$

$$\epsilon_r = 0.5$$

$$F_v = 100 \text{ N}$$

$$F_{water} = ?$$

$$F_{water} = \frac{100 \text{ N}}{80}$$

$$= 1.25 = 1.25$$

$$\epsilon_r = 1$$

→ air / vac / free space

$$\epsilon_r = 2$$

→ Paraffin paper

$$\epsilon_r = 78.5$$

$$\epsilon_r = 80$$

→ water

$$\epsilon_r = \infty \rightarrow \text{metals}$$

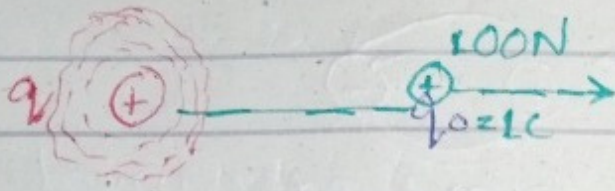
$$F_{metal} = \frac{F_v}{\infty} = 0$$

Electric Field Intensity:

$$\vec{E} = \frac{\vec{F}}{q_0} \left(\frac{N}{C} = \frac{V}{m} \right)$$

$$E = -\frac{\Delta V}{r} \left(\frac{V}{m} \right)$$

vector quantity
in direction of \vec{F}



MCQ: If $F = 100N$, $q = 1C$
 $E = ?$

Test Charge

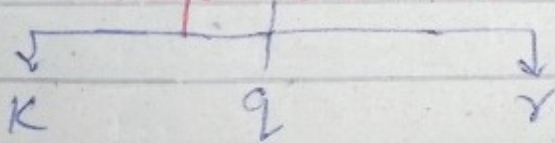
- ↳ Magnitude $\ll 0$
- ↳ Field ignorable
- ↳ $q_0 = +ve$

$$E = \frac{100}{1} = \frac{100N}{1C}$$

E field Due to Point Charge:

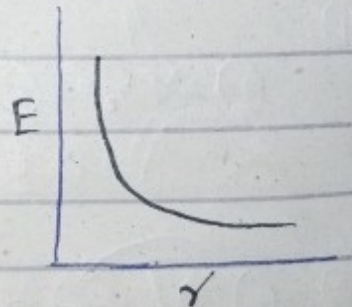
$$E = \frac{kq}{r^2}$$

Dependence



$$E \propto q$$

$$E \propto \frac{1}{r^2}$$

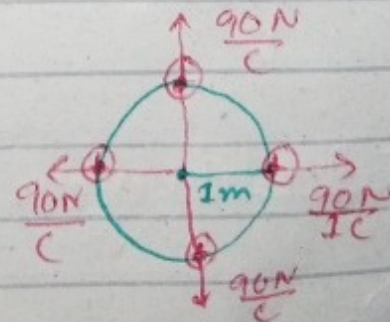


$q = 10nC$
distance = r

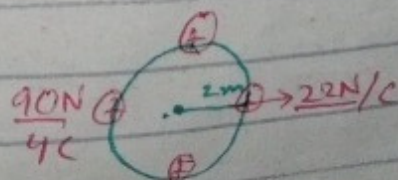
$E = ?$

$$E = \frac{kq}{r^2}$$

$$= \frac{9 \times 10^9 \times 10 \times 10^{-9}}{r^2}$$

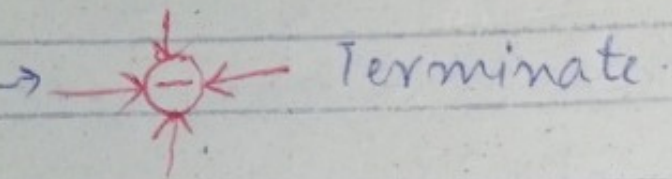
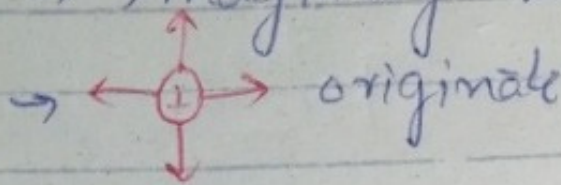


$$E = \frac{90N}{r^2}$$

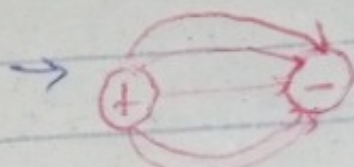
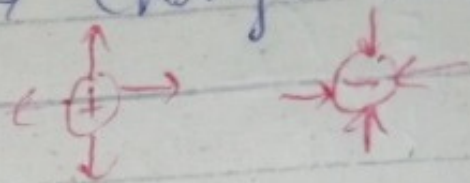


Properties of E-f.

- Michael Faraday
- Imaginary lines

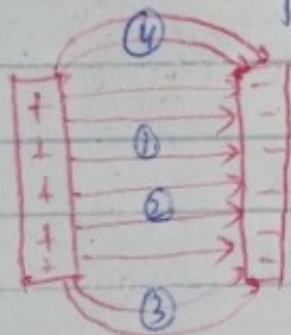


→ Charge isolation on



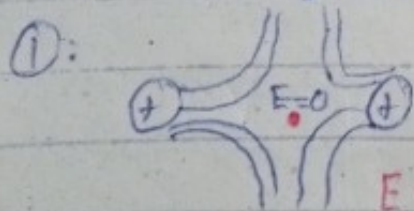
↳ lines are curved

→ Parallel plate

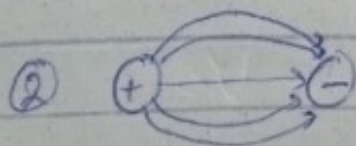


$E_1 = E_2 =$ uniform stronger
 $E_3, E_4 =$ non-uniform weaker.

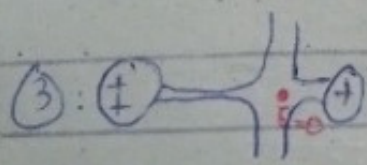
Zero Field Location:



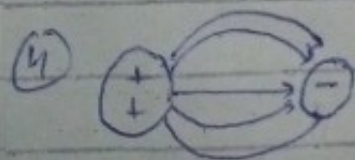
$E=0$, lies at mid



$E=0$, doesn't exist.



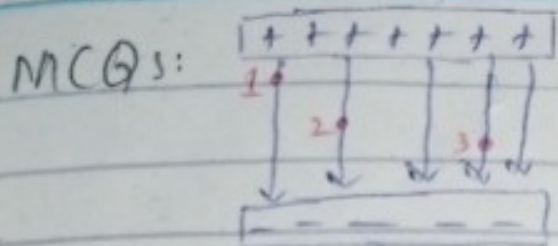
$E=0$, lies near smaller charge.



$E=0$, lies outside smaller charge.

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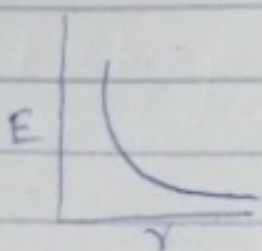
→ E · F is long range.



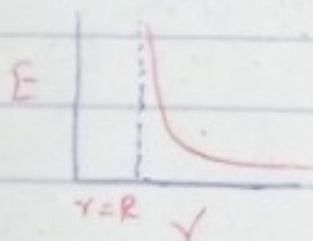
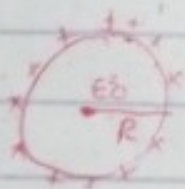
$\times E_1 > E_2 > E_3$
 $\checkmark E_1 = E_2 = E_3 \rightarrow$ uniform field

E due to point charge:

$$E = \frac{Kq}{r^2}$$



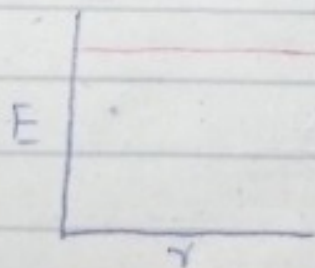
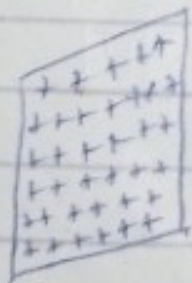
E to Hollow Charge Sphere:



E due to infinite sheet of charge:

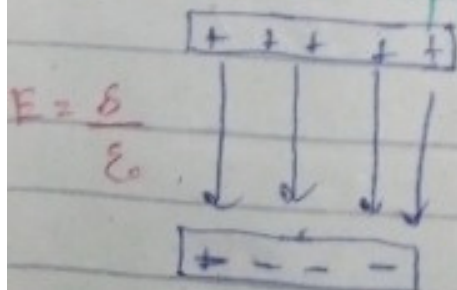
↳ So that fringing field should not provide.

$$E = \frac{\sigma}{2\epsilon_0}$$

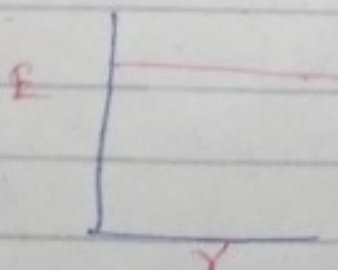


infinite

E due to oppositely charged plates:



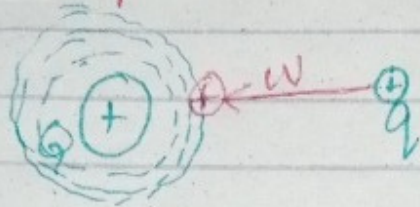
$$E = \frac{\sigma}{\epsilon_0}$$



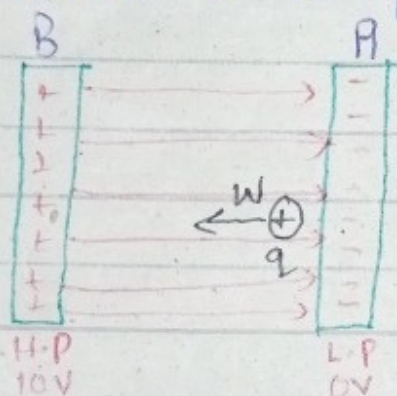
Electric Potential:

$$V = \frac{W}{q} \left(\frac{J}{C} = \frac{J \cdot C^{-1}}{Nm/C} = Volt \right)$$

↳ Work per unit charge



Potential Difference:



Work per unit charge to move it from L.P. to H.P.

$$\Delta V = \frac{W_{B \rightarrow A}}{q}$$

$$\therefore W = P \cdot E = mgh$$

$$W = E \cdot P \cdot F = U$$

$$\boxed{W_{B \rightarrow A} = \Delta U}$$

$$\Delta V = \frac{\Delta U}{q}$$

mcq: $W = 10J, q = 0.1C$
 $\Delta V = ?$

$$\Delta V = \frac{U_A - U_B}{q}$$

$$\Delta V = \frac{10}{0.1} = 100V$$

Change of E.P.F per unit charge called pd

↳ in general:

$$\Delta V = \frac{W}{q}$$

$$\Delta V = 10, q = 0.1, W = ?$$

$$W = q \Delta V$$

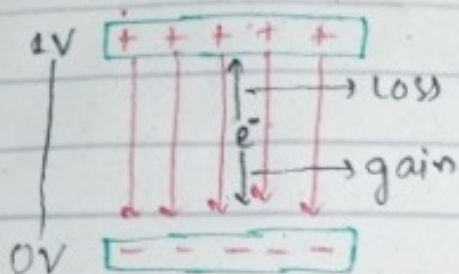
$$= 0.1 \times 10$$

$$= 1J$$

$$\boxed{= 1J}$$

Electron Volt:

→ Energy gain or lost by an electron as it moves in p.d of 1V (smaller unit of energy)



$$W = q \Delta V$$

$$W = \Delta P \cdot E \quad \downarrow \text{gain}$$

$$\Delta P \cdot E = q \Delta V$$

$$W = \Delta K \cdot E \quad \downarrow \text{loss}$$

$$\Delta K \cdot E = q \Delta V$$

$$\Delta K \cdot E = q \Delta V$$

$$\therefore q = 1e, \Delta V = 1V$$

$$\Delta K \cdot E = (1e)(1V)$$

$$\Delta K \cdot E = 1eV = 1.6 \times 10^{-19} J$$

$$1eV = 1.6 \times 10^{-19} J$$

MCQ:

$$K \cdot E = W = 4eV$$

$$q = 2 \mu C$$

$$\Delta V = ?$$

$$\Delta V = \frac{W}{q} = \frac{4 \times 10^{-20}}{2 \times 10^{-6}} = 2 \times 10^{-14}$$

$$= 32 \times 10^{-14}$$

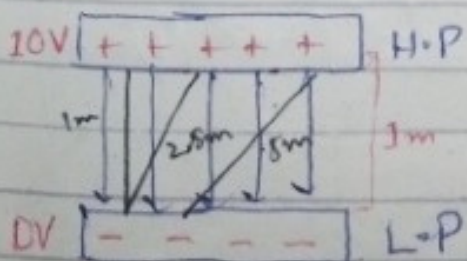
$$\Delta V = 3.2 \times 10^{-13}$$

Potential Gradient:

The maximum value of rate of change of potential w.r.t displacement.

$$E = - \left(\frac{\Delta V}{\Delta r} \right)_{\text{max}}$$

-ive sign, direction of electric field is towards decreasing potential.



$$\Delta V = 10V$$

$$\Delta r = 3m$$

$$E = - \left(\frac{10}{3} \right) \frac{V}{m}$$

$$E = -10$$

$$2.5$$

$$E = -4 \text{ mV}$$

$$E = -\frac{10}{5}$$

$$E = -2 \text{ Vm}^{-1}$$

Equipotential Surface:

$$\rightarrow V = \text{constant}$$

$$\rightarrow \Delta V = 0$$

$$\rightarrow E = -\frac{\Delta V}{\Delta r}$$

$$\rightarrow E = 0$$

\rightarrow Work done $E \cdot F$ inside the surface is 0.

MCG:

$$q = 10 \text{ nC}$$

$$V = \frac{kq}{r}$$

$$V = \frac{9 \times 10^9 \times 10 \times 10^{-9}}{r}$$

$$V = \frac{90}{r}$$

$$\rightarrow V = \text{constant}$$

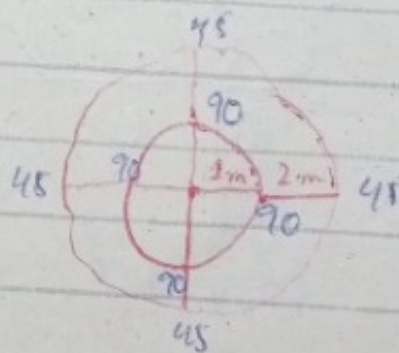
$$\rightarrow \Delta V = 0$$

$$\rightarrow \Delta V = \frac{W}{q}$$

$$\rightarrow 0 = \frac{W}{q}$$

$$\rightarrow W = 0$$

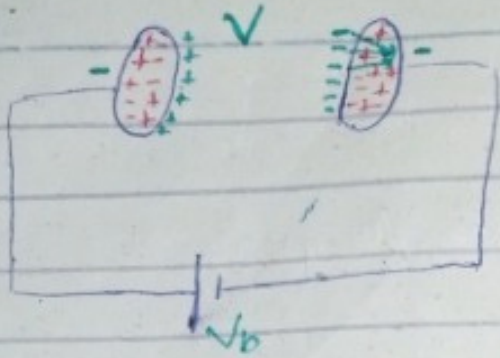
\rightarrow Work done on equipotential surface is 0.



Capacitor:

\rightarrow Device used to store charge.

\rightarrow Capacitor stores energy in form of electric field.



$$q \propto V$$

$$q = CV$$

C: capacitance
 $C \rightarrow$ independent to q & V

MCG: If charge on capacitor plates become double. If 'C' = ?

a: decrease

b: increase

$$C = \frac{q}{V} = \frac{2q}{2V} = \frac{q}{V}$$

same.

c: same

d: None

MCG: Which unit is ~~largest~~ suitable for largest capacitance?

a: 1F

b: 8F

Largest in world:

50,000 μ F

c: 10F

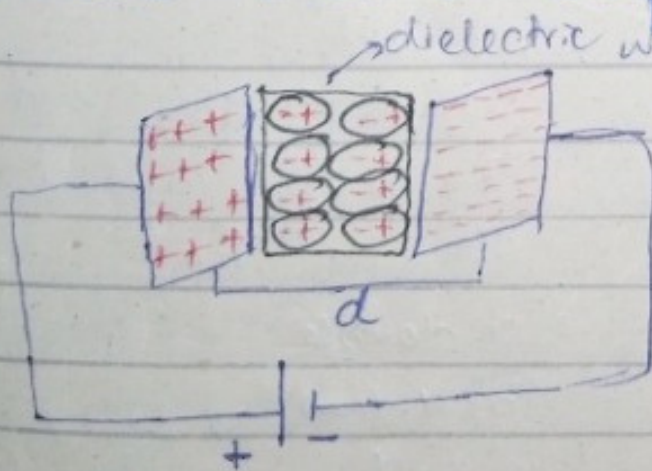
d: None

0.05 F

Unit:

$$C = \frac{Q}{V} = \text{Farad}$$

Parallel Plate Capacitor:



on inserting dielectric b/w plates, its capacitance increases by factor ϵ_r .

$$C_{med} = \frac{A \epsilon_0 \epsilon_r}{d}$$

$$C_{vac} = \frac{A \epsilon_0}{d}$$

$$C_{med} = C_{vac} \epsilon_r$$

for water

$$C_{water} = 10F \times 80$$

$$= 800F$$

$C_{vac} = 10F$

Energy stored in Capacitor in form of Electric field:

$$U = \frac{1}{2} \epsilon_0 \epsilon_r E^2 Ad$$

$U \propto E^2$ → By putting dielectric b/w plates the E will decrease hence energy will decrease
 ↳ By increasing capacitance the energy will decrease

Energy Density: (J/m^3)

$$U' = \frac{U}{\text{Volume}} = \frac{1}{2} \epsilon_0 \epsilon_r E^2 \frac{Ad}{Ad}$$

$$U' = \frac{1}{2} \epsilon_0 \epsilon_r E^2$$

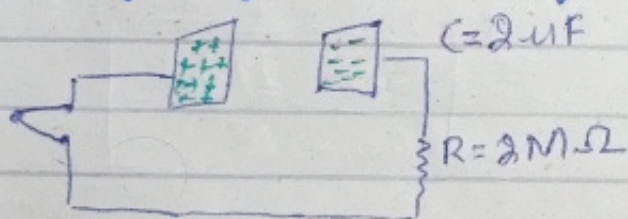
mcq: Unit of Equation $\frac{1}{2} \epsilon_0 \epsilon_r E^2 Ad$

a: J c: Jm.

b: Jm^3 d none.

⊗ Energy will always be joule.

Charging of Capacitor:



Time constant:

$$t = RC$$

↓ ↓ ↓
s = Ω F

$$t = 2 \times 10^6 \times 2 \times 10^{-6}$$

$$t = 4s$$

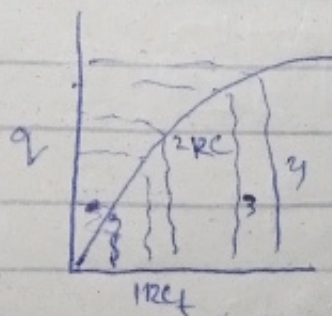
1RC → 63%

2RC → 86%
↓ 22%

3RC → 94%
↓ 8%

4RC → 98%
↓ 4%

5RC → 99%
↓ 1%



∴ A capacitor can't charge 100%

$$\epsilon_r = \frac{C_{med} \epsilon}{C_{vac}}$$

① $E \downarrow$ → As insulator is placed b/w plates

$$\textcircled{2} \downarrow E = \frac{\downarrow S}{\epsilon_0}$$

$$\textcircled{3} \downarrow E = \frac{\downarrow V}{d} \rightarrow \text{separation b/w plates will remain same}$$

④: $q = \text{constant}$

$$q = CV$$

constant

$$\uparrow C \propto \frac{1}{\downarrow V}$$

$$\epsilon_r = \frac{F_{vac}}{F_{med}} = \frac{V_{vac}}{V_{med}} = \frac{C_{med}}{C_{vac}} = \frac{Q_{med}}{Q_{vac}}$$

Energy Stored in Capacitor:

$$E = \frac{1}{2} qV$$

$$q = CV$$

$$V = \frac{q}{C}$$

$$E = \frac{1}{2} CV^2$$

$$E = \frac{1}{2} \frac{q^2}{C}$$

$$E = \frac{1}{2} qV = \frac{1}{2} CV^2 = \frac{1}{2} \frac{q^2}{C}$$

3) $E = \frac{1}{2} qV$, and charge on capacitor

" $q = 2q$ " $E = ?$

a: double

$\therefore q \propto V$

b: 4-times

$$E' = \frac{1}{2} (2q)(2V)$$

c: half

d: $\frac{1}{4}$ times

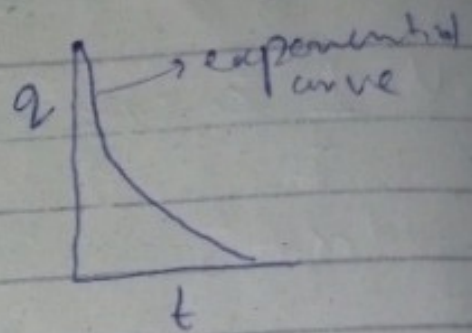
$$E' = 4 \left(\frac{1}{2} qV \right)$$

$$E' = 4E$$

As charge increases will increase

Discharging Of Capacitors:

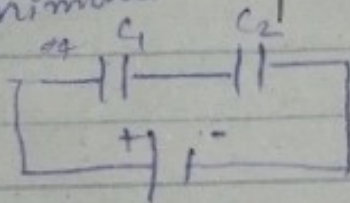
- 1 RC \longrightarrow 37%
- 2 RC \longrightarrow 15%
- 3 RC \longrightarrow 5%
- 4 RC \longrightarrow 1.5%
- 5 RC \longrightarrow 0.05%



Combinations Of Capacitors:

1: Series Combination

~~Maximum~~ ^{or} ~~Minimum~~ Capacitance:



$$C_{eq} = \frac{1}{\frac{1}{C_1} + \frac{1}{C_2}}$$

$$C_{eq} = \frac{C}{n}$$

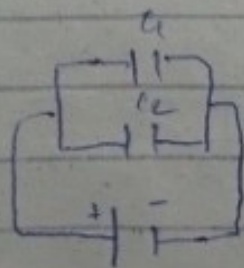
eggs Ratio of $\frac{C_{max}}{C_{min}} = ?$

$$\frac{C_{max}}{C_{min}} = \frac{nC}{\frac{C}{n}}$$

$$\boxed{\frac{C_{max}}{C_{min}} = n^2}$$

2: Parallel Combination:

~~Minimum~~ ^{or} ~~Maximum~~ Capacitance:



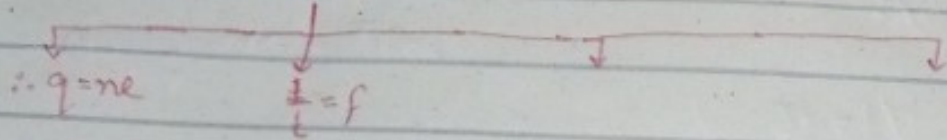
$$C_{eq} = C_1 + C_2$$

$$C_{eq} = nC$$

Current Electricity:

↳ Study of charges in motion.
 Path of flow of charges called current.

$$I = \frac{q}{t} \left(\frac{C}{s} = A \rightarrow SI \right)$$



$$I = \frac{ne}{t}$$

$$I = qf$$

$$n = \frac{It}{e}$$

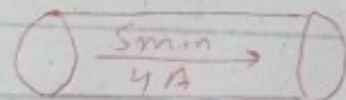
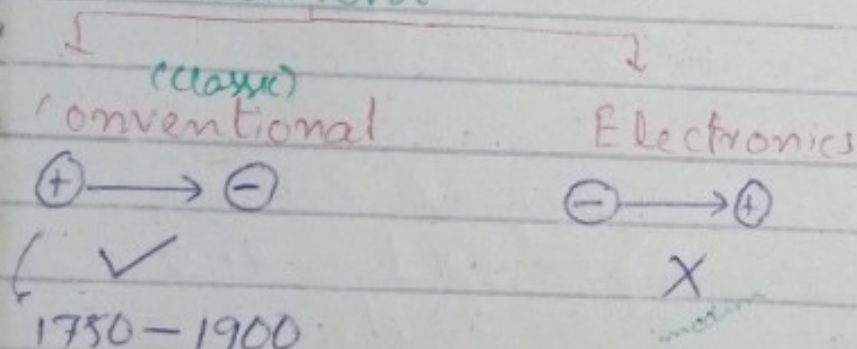
$$\frac{I}{e} = \frac{n}{t}$$

C.G.S unit of current (stat-A)

$$1A = 3 \times 10^9 \text{ stat-A}$$

MCG: $I = 4A, t = 5 \text{ min}$
 $n = ?$

Current



$$n = \frac{It}{e}$$

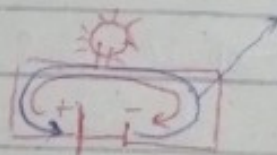
$$n = \frac{4 \times 300}{1.6 \times 10^{-20}} =$$

$$n = \frac{300 \times 10^{20}}{4}$$

$$n = 7.5 \times 10^{21} \text{ es}$$

1750-1900
 volta

H → L



Charge Carriers:

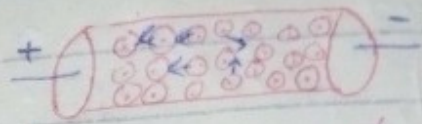
- 1: Conductors → only free e^-
- 2: Semi Conductors → holes + e^-
- 3: Gas → ions + e^-
- 4: Electrolytes → ions only

Drift Velocity:

The maximum constant velocity attain by an electron as it moves

$$1 \text{ cm}^3 = 10^{23} \text{ free } e^-$$

in presence of electric field.



$$t = 1 \text{ s}$$

$$d = 1 \text{ mm}$$

$$v_d = \frac{d}{t} = 1 \text{ mm/s}$$

$$v_d = 10^{-3} \text{ m/s}$$

$$v_d = 10^{-3} \text{ m/s}$$

$$v_d \propto \frac{1}{A} \propto \frac{1}{r^2} \propto \frac{1}{d^2}$$

$$v_e = 10^6 / 10^8$$

$$v_d = \frac{I}{neA}$$

n : electron density
 n = electron volume

$$v_d = \frac{V}{neR \pi r^2}$$

$A = \pi r^2$
 $r = \frac{d}{2}$

$$v_d = \frac{V}{neR \pi \frac{d^2}{4}}$$

Resistance:

↳ Opposition offered by atoms to the flow of charges.

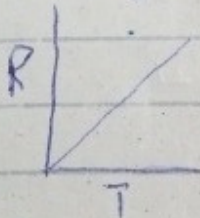
Resistance & Temp

For Conductors

$$R \propto T$$

→ free e^-
 10^{23}

by giving $100 e^-$ → no effect



For Semiconductors

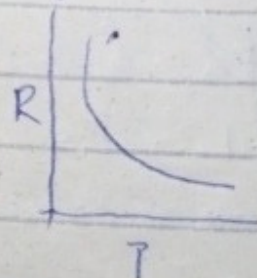
$$R \propto \frac{1}{T}$$

2023

→ free e^-

20-30

adding e^- will have effect



Ohms Law:

The current is directly proportional to voltage if temperature of conductor remains same.

$$I \propto V$$

$$I = (\text{constant}) V$$

$$V \propto I R$$

$$I = \left(\frac{1}{R}\right) V \quad R = \text{resistance.}$$

$$IR = V$$

$$I = GV \quad \therefore \frac{1}{R} = G$$

MCG:

9m ohms law the proportionality constant is:

a: R b: $\frac{1}{R}$ c: G d: b, c

$$G = \frac{1}{R} \Rightarrow \boxed{GR = 1}$$

$$f = \frac{1}{T} \Rightarrow \boxed{fT = 1}$$

$\rightarrow R$ is independent of I & V :

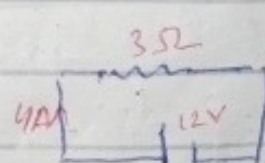
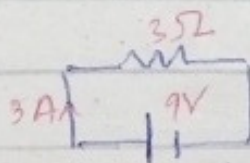
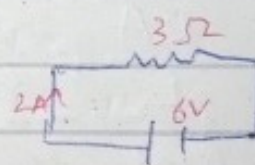
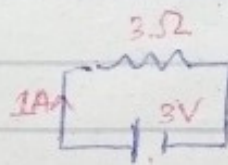
MCG:

9b $I = 2A, R = ?$

$$R = \frac{V}{I} \Rightarrow R = \frac{2V}{2A} \therefore 1 \Omega \quad \boxed{R = \frac{V}{I}}$$

Characteristics

V	I	R
3V	1A	3Ω
6V	2A	3Ω
9V	3A	3Ω
12V	4A	3Ω



Limitations:

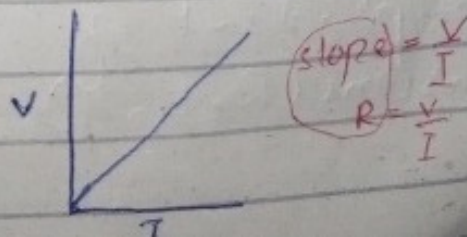
i: Temp = constant

ii: Resistance = constant

\rightarrow Ohms law is not applicable for transformer.

$T \neq$ constant

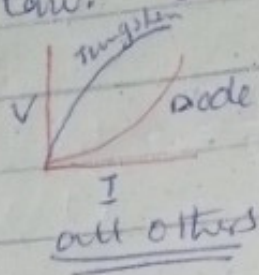
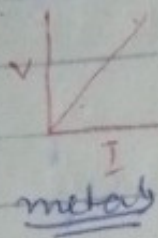
Area = $\frac{IV}{I} = \text{Power}$



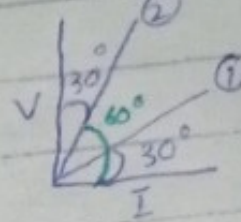
Ohmic Non Ohmic:

→ obeys ohms law

↳ not obey ohms law.



incq: $R_1 : R_2 = ?$



∴ $\tan \theta$ is w.r. to x-axis.

$$R_1 = \frac{\tan 30^\circ}{1} = \frac{1}{\sqrt{3}}$$

$$R_2 = \frac{\tan 60^\circ}{1} = \sqrt{3}$$

$$\frac{R_1}{R_2} = \frac{1}{(\sqrt{3})^2} = \frac{1}{3}$$

Resistance & Resistivity:

$$R \propto L \quad \left(\begin{array}{|c|} \hline R \\ \hline L \end{array} \right) A$$

$$\left(\begin{array}{|c|} \hline 2R \\ \hline 2L \end{array} \right) A$$

$$R \propto \frac{1}{A} \quad \left(\begin{array}{|c|} \hline R \\ \hline L \end{array} \right) A$$

$$\left(\begin{array}{|c|} \hline \frac{R}{2} \\ \hline L \end{array} \right) 2A$$

$$R = \rho \frac{L}{A}$$

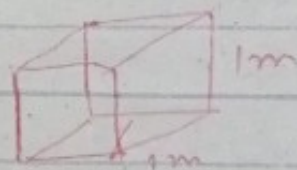
∴ ρ specific resistance

Resistivity (or) $(R = \rho)$
Resistance of 1m wire.

$$\rho = \frac{RA}{L} \left(\frac{\Omega m^2}{m} \right)$$

if $A = 1m^2, L = 1m$

$$\rho = \frac{R \times 1m^2}{1m}$$



$$\rho = R (\Omega m)$$

if wire is cut into two parts. $\rho = ?$, $R = ?$

ρ = same, R = half

Dependence:

↳ Nature

↳ Temp

↳ Independent of dimensions (R, L, A)

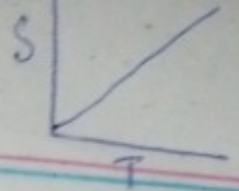
$$\rho = \frac{R A}{L}$$

$$\frac{L}{2}$$

$$\rho = \frac{RA}{L}$$

Stretching:

$$S \propto T$$



If the length of wire becomes double by stretching. If $R = ?$

a: double

b: Half

c: 4 times

d: same

$$\text{Original wire: } L, A$$

$$\text{Stretched wire: } 2L, A/2$$

$$R = \frac{\rho L}{A} \rightarrow R = \frac{\rho (2L)}{A/2} \quad R' = 4R$$

Short cut:

$$R = \frac{\rho L}{A}$$

$$R = \frac{\rho L}{A} \times \frac{L}{L}$$

$$R = \frac{\rho L}{A} \times \frac{A}{A}$$

$$R = \frac{\rho L^2}{AL}$$

$$R = \frac{\rho LA}{A^2}$$

$$\therefore AL = V$$

$$R \propto L^2$$

$$R \propto \frac{1}{A^2}$$

Coefficient Of Resistance:

The fractional change in resistance per kelvin temperature.

$$t_0 = 0^\circ\text{C} \\ R_0 = 100$$

$$t = 10^\circ\text{C} \\ R_t = 200$$

$$\alpha = \frac{R_t - R_0}{R_0 \Delta t}$$

change in temperature

$$\alpha = \frac{200 - 100}{100(10 - 0)}$$

$$\alpha = \frac{R_t - R_0}{R_0(t - t_0)}$$

$$\alpha = \frac{100}{100(10)} = \frac{1}{10} = 0.1 \text{ K}^{-1} \text{ or } ^\circ\text{C}^{-1}$$

$$\alpha = \frac{1}{\Delta t}$$

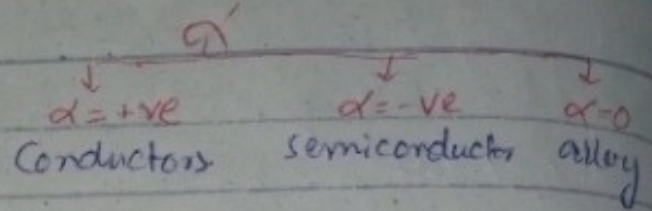
$$\alpha \rightarrow \text{C}^{-2} \text{osk}^{-1}$$

#

$$\alpha R_0 \Delta t = R_t - R_0$$

$$R_t = R_0 + \alpha R_0 \Delta t$$

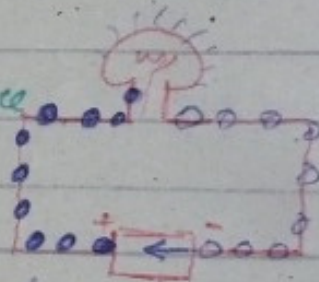
$$R_t = R_0 (1 + \alpha \Delta t)$$



Electromotive Force:

↳ The energy supplied by a unit +ve charge to move it from -ve to +ve terminal inside.

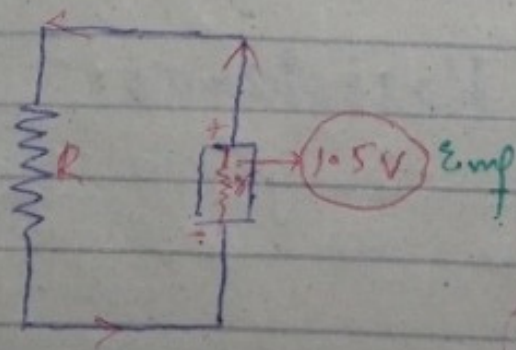
* Battery is not source of charges it just push or pull charges.



Emf = $\frac{\text{Energy supplied}}{\text{charge}}$

$$\text{Emf} = \frac{W}{q} \left(\frac{J}{C} = \text{volt} \right)$$

↳ unit of emf.



$$V = I R_{eq}$$

$$V = I (R + r)$$

$$\mathcal{E} = IR + Ir$$

$$I = \frac{\mathcal{E}}{R + r}$$

$$\frac{\mathcal{E}}{I} = R + r$$

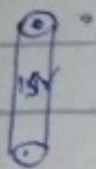
$$\mathcal{E} = V_t + I r$$

$$V_t = \mathcal{E} - I r$$

Open circuit

$$I = 0$$

$$V_t = \mathcal{E}$$



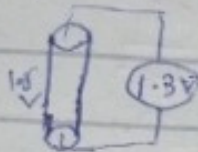
$$\mathcal{E} = V_t$$

Close circuit

$$I \neq 0$$

$$V_t = \mathcal{E} - I r$$

$$\mathcal{E} > V_t$$



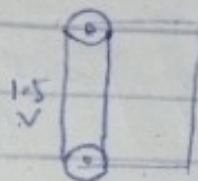
Short circuit

$$I = \text{max}$$

$$\mathcal{E} = I r$$

$$V_t = \mathcal{E} - \mathcal{E}$$

$$V_t = 0$$



When battery is being charged

$$I = -I$$

$$V_t = \mathcal{E} - (-I r)$$

$$V_t = \mathcal{E} + I r$$

$$V_t > \mathcal{E}$$

Power:

$$P = \frac{\text{Energy}}{t}$$

$$P = \frac{W}{t}$$

$$\therefore V = \frac{W}{Q}$$

$$P = \frac{V Q}{t}$$

$$\therefore \frac{Q}{t} = I$$

$$P = I V$$

$$P = I V$$

Series

$$\frac{1}{P_{eq}} = \frac{1}{P_1} + \frac{1}{P_2}$$

Parallel

$$P_{eq} = P_1 + P_2$$

$$P = I^2 R$$

Child toys

$$P = \frac{V^2}{R}$$

Housing wire.

Heat:

$$P = \frac{E}{t} = \frac{H}{t}$$

$$\frac{H}{t} = I^2 R \Rightarrow H = I^2 R t$$

$P_{rated} = 100 \text{ watt}$
 $V_{rated} = 220 \text{ V}$

Rated?

If 100 watt, 220V bulb is connected by a battery of 110V then power consume will be?

$P_{rated} = 100 \text{ watt}$
 $V_{rated} = 220 \text{ V}$
 $V_s = 110 \text{ V}$
 $P_c = ?$

$P_{rated} \propto V_{rated}^2$
 $P_{consume} \propto V_{supply}^2$
 $R \quad P = \frac{V^2}{R}$

$\frac{P_c}{P_r} = \frac{V_s^2}{V_r^2}$

$P_c = \frac{V_s^2 \times P_r}{V_r^2} \Rightarrow \frac{(110)^2 \times 100}{(220)^2}$

$P_c = \frac{1}{2} \times \frac{1}{2} \times 100 = \frac{25}{4} \Rightarrow \boxed{25 \text{ watt}}$

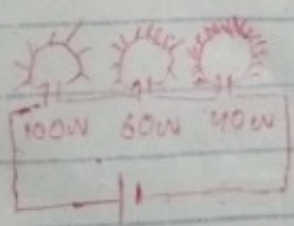
Brightness

$P_{rated} \propto \frac{1}{R}$ $R \propto \frac{1}{P_{rated}}$

$B \rightarrow P$

Series

$P = I^2 R$
 $B = I^2 R$
 $I = \text{constant}$
 $B \propto R \propto \frac{1}{P_{rated}}$



$B \propto \frac{1}{P_{rated}}$

Parallel

$P = \frac{V^2}{R}$
 $B = \frac{V^2}{R}$
 $V = \text{constant}$
 $B \propto \frac{1}{R} \propto P_{rated}$



$B \propto P_{rated}$

@isamiqamar